

Allowable Loads on Beams without Lateral Support

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BEAMS WITH UNBRACED lengths along the compression flange greater than L_c or L_u require the designer to consider factors other than section modulus alone, since torsional properties and the lateral bending strength of the compression flange influence the ability of the beam to resist lateral buckling.

This paper presents tables developed to aid the designer in rapidly selecting the most economical **WF** or **I** section for laterally unsupported beams.

NOMENCLATURE

- A_f = Area of compression flange, sq in.
 A_w = Area of web of steel section, sq in.
 b_f = Flange width, in.
 C = Constant determined from beam properties
 C_b = Bending coefficient dependent upon moment gradient
 = 1 for simple bending
 = 1.75 for cantilever ends
 = $1.75 - 1.05(M_1/M_2) + 0.3(M_1/M_2)^2 \leq 2.3$
 for beams or beam segments with moments at the points of lateral support
 d = Depth of steel section, in.
 F_b = Allowable bending stress, ksi
 f_b = Computed bending stress, ksi
 F_y = Specified minimum yield point of steel being used, ksi
 I_f = Moment of inertia of the compression flange, in.⁴. Use $1/2$ of the I_y values given in the AISC Manual.
 I_y = Moment of inertia about the y -axis
 l = Unbraced length, in.
 L = Unsupported span length, ft
 L_c = Maximum unbraced length of the compression flange at which the allowable bending stress may be taken at $0.66 F_y$, ft

- L_u = Maximum unbraced length of the compression flange at which the allowable bending stress may be taken at $0.60 F_y$, ft
 M = Moment, ft-kips
 M_1 = Smaller end moment on unbraced length of beam, ft-kips
 M_2 = Larger end moment on unbraced length of beam, ft-kips
 r' = Radius of gyration of the tee section, comprising the compression flange plus $1/6$ of the web area, about an axis in the plane of the web, in.
 = $\sqrt{I_f/(A_f + 1/6 A_w)}$
 R = Reaction, kips
 S = Section modulus, in.³

SPECIFICATION REQUIREMENTS

The AISC Specification permits an allowable bending stress, F_b , of 24 ksi for compact sections of ASTM A36 steel when the unbraced length along the compression flange is equal to or less than L_c . $L_c = (13/12)b_f$.

The Specification limits the allowable bending stress, F_b , for both compact and non-compact sections of A36 steel to 22 ksi when the unbraced length along the compression flange is greater than L_c , but equal to or less than L_u . $L_u = (545/12) \times d/A_f$ and $L_c < L \leq L_u$.

When the unbraced length of the compression flange is greater than L_u the allowable bending stress, F_b , must be reduced in accordance with the provisions of Section 1.5.1.4.5 of the Specification, and may not exceed the larger value as given by the following Formulas, nor $0.60 F_y$. For A36 steel,

$$F_b = 22,000 - \frac{0.672}{C_b} \left(\frac{l}{r'} \right)^2 \leq (0.60 F_y = 22 \text{ ksi}) \quad \text{Formula (4)}$$

$$F_b = \frac{12,000,000}{L \times d/A_f} \leq 22 \text{ ksi} \quad \text{Formula (5)}$$

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An inspection of the allowable moment charts on pages 2-48 to 2-53 of the AISC Manual reveals that Formula (5) governs the allowable stress in most instances when I and W shapes are used and the unbraced length exceeds L_u . In most cases where Formula (4) would govern, the decrease in allowable moments by the use of Formula (5) would be small. In every case the results would be conservative.

MATHEMATICAL DERIVATION

From Formula (5):

$$f_b = \frac{M}{S} = \frac{12,000,000}{L \times d/A_f}$$

$$\frac{M \times L}{12,000,000} = \frac{S}{d/A_f}$$

Let

$$C = \frac{S}{d/A_f}$$

Then,

$$C = \frac{12M \times L}{1,000} \quad \text{Equation (1)}$$

TABLE PREPARATION

Tabular listings of C , S , L_c , L_u , d/A_f and r' are shown in Table 1 for all W and I shapes listed in the AISC Manual of Steel Construction, 6th Edition, pages 1-6 through 1-25, as well as the six new light beam sections now being rolled by Bethlehem Steel Corp. and U. S. Steel Corp. Shapes are listed in the order of descending C -values to aid in selecting the most economical section.

The r' values were determined using $I_f = \frac{1}{2}I_y$ in the formula given in the Nomenclature.

USE OF TABLE 1

Example 1—Select the most economical simple beam to support a uniform load of 2 kips/lin ft over a span of 20 ft. Lateral bracing is provided at the supports. Use A36 steel. See Fig. 1.

Solution:

$$F_b = 22 \text{ ksi}$$

$$R = 2 \times \frac{20}{2} = 20 \text{ kips}$$

$$M = 2 \times \frac{20}{8} = 100 \text{ ft-kips}$$

$$\text{Req'd } S = 100 \times \frac{12}{22} = 54.5 \text{ in.}^3$$

$$\text{Req'd minimum } C = \frac{12 \times M \times L}{1,000} =$$

$$\frac{12 \times 100 \times 20}{1,000} = 24.0 \quad \text{Equation (1)}$$

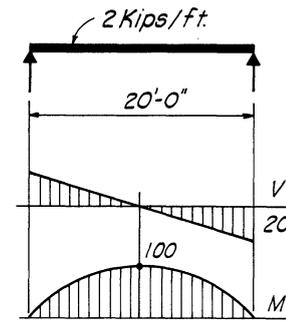


Figure 1

1. The minimum required C as computed by Equation (1) is 24.0. Therefore, select from Table 1 the lightest steel section with C equal to or greater than the computed C and with S equal to or greater than the required S , 54.5 in.³.

From Table 1:

C	Shape	S	L_c	L_u	d/A_f	r'	Re- marks
25.7	18W55	98.2	8.2	11.9	3.82	1.90	OK
24.4	18I70	101.9	6.8	10.9	4.17	1.40	OK
24.2	14W48	70.2	8.7	15.7	2.90	2.16	USE
24.1	10W45	49.1	8.7	22.3	2.04	2.20	NG

2. The 10W45 is inadequate, because the furnished S of 49.1 is less than the 54.5 in.³ required if the beam was fully braced at intervals equal to or less than L_u .
3. From Formula (4), $F_b = 22,000 - 0.679/C_b(l/r')^2$, and by inspection of the table the least amount of reduction in F_b occurs when the r' value is the largest. Therefore; the 14W48 ($r' = 2.16$) would be the most economical and least weight section.
4. For normal cases, calculations need go no further. For illustrative purposes, however, compute F_b by Formulas (4) and (5) for the 14W48 with $S = 70.2$, $r' = 2.16$, $d/A_f = 2.90$.

$$F_b = 22,000 - \frac{0.679}{1} \left(\frac{20 \times 12}{2.16} \right)^2 = 13.62 \text{ ksi}$$

Formula (4)

$$F_b = \frac{12,000,000}{20 \times 12 \times 2.90} = 17.24 \text{ ksi (governs)}$$

Formula (5)

5. The permitted allowable stress is 17.24 ksi (the largest of the values computed by Formulas (4) and (5)).

$$f_{\text{actual}} = \frac{100 \times 12}{70.2} = 17.1 < 17.24 \quad \text{OK}$$

6. The designer should check for shear as well as architectural considerations.

TABLE 1 (A36 steel)

C	Shape	S	L _c	L _u	d/A _f	r'	C	Shape	S	L _c	L _u	d/A _f	r'
1916.6	14WF426	707.4	18.1	123.1	0.329	4.65	145.0	*14BP117	172.6	16.1	42.7	1.19	4.03
1693.0	14WF398	656.9	18.0	117.1	0.388	4.62	144.2	10WF112	126.3	11.3	51.8	0.876	2.89
1484.3	14WF370	608.1	17.9	110.8	0.410	4.58	139.3	18WF114	220.1	12.8	28.8	1.58	3.09
1286.0	14WF342	559.4	17.7	104.4	0.435	4.55	138.5	24WF120	299.1	13.1	21.0	2.16	3.09
1103.2	14WF314	511.9	17.6	97.9	0.464	4.51	136.3	*14WF103	163.6	15.8	41.6	1.20	4.03
1024.5	14WF320	492.8	18.1	94.4	0.481	4.58	135.1	12WF106	144.5	13.3	42.4	1.07	3.38
934.7	14WF287	465.5	17.5	91.2	0.498	4.48	133.5	21WF112	249.6	14.1	24.3	1.87	3.35
843.6	36WF300	1105.1	18.0	34.7	1.31	4.29	132.3	30WF132	379.7	11.4	15.8	2.87	2.62
804.9	14WF264	427.4	17.4	85.5	0.531	4.45	120.5	33WF130	404.8	12.5	13.5	3.36	2.80
736.6	36WF280	1031.2	18.0	32.5	1.40	4.27	118.2	18WF105	202.2	12.8	26.6	1.71	3.07
707.1	14WF246	397.4	17.3	80.8	0.562	4.43	118.2	12WF99	134.7	13.2	39.8	1.14	3.37
659.0	14WF237	382.2	17.2	78.3	0.580	4.42	117.3	24WF110	274.4	13.0	19.4	2.34	3.06
625.7	36WF260	951.1	17.9	29.9	1.52	4.23	117.0	36WF135	438.6	—	12.1	3.75	2.84
616.1	14WF228	367.8	17.2	76.1	0.597	4.41	117.0	10WF100	112.4	11.2	47.3	0.961	2.87
570.6	14WF219	352.6	17.1	73.5	0.618	4.39	115.8	*14WF95	150.6	15.8	38.6	1.30	4.02
550.9	36WF245	892.5	17.9	28.1	1.62	4.20	115.1	30WF124	354.6	11.4	14.8	3.08	2.60
537.2	33WF240	811.1	17.2	30.1	1.51	4.07	111.4	*14BP102	150.4	16.0	37.0	1.35	4.00
531.7	14WF211	339.2	17.1	71.2	0.638	4.38	103.3	12WF92	125.0	13.2	37.5	1.21	3.35
492.3	14WF202	324.9	17.1	68.8	0.660	4.37	102.8	27WF114	299.2	10.9	15.6	2.91	2.52
482.9	36WF230	835.5	17.8	26.3	1.73	4.17	102.5	16WF96	166.1	12.5	28.1	1.62	3.02
451.9	14WF193	310.0	17.0	66.2	0.686	4.36	99.1	18WF96	184.4	12.8	24.4	1.86	3.04
448.8	33WF220	740.6	17.1	27.5	1.65	4.03	98.6	*14WF87	138.1	15.7	35.6	1.40	4.01
424.8	30WF210	649.9	16.4	29.7	1.53	3.89	97.6	30WF116	327.9	11.4	13.5	3.36	2.57
414.9	14WF184	295.8	17.0	63.7	0.713	4.35	96.5	24WF100	248.9	13.0	17.6	2.58	3.03
402.4	12WF190	263.2	13.7	69.4	0.654	3.51	94.1	10WF89	99.7	11.1	42.8	1.06	2.84
379.4	14WF176	281.9	16.9	61.1	0.743	4.34	92.6	24I120	250.9	8.7	16.8	2.71	1.90
367.9	33WF200	669.6	17.1	25.0	1.82	3.99	92.3	33WF118	358.3	—	11.7	3.88	2.74
346.8	30WF190	586.1	16.3	26.9	1.69	3.85	89.7	12WF85	115.7	13.1	35.2	1.29	3.34
344.0	14WF167	267.3	16.9	58.5	0.777	4.33	86.1	14WF84	130.9	13.0	29.9	1.52	3.31
312.1	14WF158	253.4	16.8	55.9	0.812	4.32	85.8	*14BP89	131.2	15.9	32.6	1.53	3.97
302.3	27WF177	492.8	15.3	27.9	1.63	3.62	85.5	16WF88	151.3	12.5	25.7	1.77	3.00
297.9	12WF161	222.2	13.6	60.9	0.746	3.47	84.9	24I105.9	234.3	8.5	16.5	2.76	1.90
282.5	30WF172	528.2	16.2	24.3	1.87	3.81	81.4	27WF102	266.3	10.9	13.9	3.27	2.49
282.3	14WF150	240.2	16.8	53.4	0.850	4.30	80.0	30WF108	299.2	11.4	12.2	3.74	2.42
277.7	36WF194	663.6	13.1	19.0	2.39	3.01	79.0	21WF96	197.6	9.8	18.2	2.50	2.30
266.8	24WF160	413.5	15.3	29.3	1.55	3.65	77.1	12WF79	107.1	13.1	32.7	1.39	3.33
253.3	14WF142	226.7	16.2	50.7	0.895	4.29	74.3	14WF78	121.1	13.0	27.9	1.63	3.30
246.9	27WF160	444.5	15.2	25.3	1.80	3.59	72.0	24WF94	220.9	9.8	14.8	3.07	2.28
243.6	36WF182	621.2	13.1	17.8	2.55	3.00	71.8	10WF77	86.1	11.0	37.8	1.20	2.82
229.5	14WF136	216.0	16.0	48.3	0.941	4.08	68.5	18WF85	156.1	9.6	19.9	2.28	2.29
217.8	24WF145	372.5	15.2	26.6	1.71	3.62	67.3	27WF94	242.8	10.8	12.6	3.61	2.46
212.9	21WF142	317.2	14.2	30.5	1.49	3.42	64.1	*12WF72	97.5	13.0	32.9	1.52	3.32
212.1	36WF170	579.1	13.0	16.7	2.73	2.97	63.6	30WF99	269.1	—	10.7	4.23	2.48
208.6	12WF133	183.5	13.4	51.9	0.875	3.42	62.6	10WF72	80.1	11.0	35.5	1.28	2.81
204.5	27WF145	402.9	15.1	23.1	1.97	3.55	62.4	14WF74	112.3	10.9	25.3	1.80	2.75
202.6	14WF127	202.0	15.9	45.6	0.997	4.07	58.9	16WF78	127.8	9.3	20.9	2.17	2.23
184.0	36WF160	541.0	13.0	15.5	2.94	2.94	58.1	*14BP73	107.5	15.8	27.0	1.85	3.94
178.7	14WF119	189.4	15.9	42.9	1.06	4.06	57.4	*12BP74	93.5	13.2	30.6	1.63	3.29
177.5	33WF152	486.4	12.5	16.6	2.74	2.88	57.3	21WF82	168.0	9.7	15.5	2.93	2.27
172.2	21WF127	284.1	14.1	27.5	1.65	3.39	56.9	18WF77	141.7	9.5	18.3	2.49	2.27
171.3	24WF130	330.7	15.2	23.6	1.93	3.57	56.6	24WF84	196.3	9.8	13.1	3.47	2.25
169.7	12WF120	163.4	13.3	47.2	0.963	3.40	53.8	10WF66	73.7	11.0	33.2	1.37	2.80
157.6	36WF150	502.9	13.0	14.2	3.19	2.91	52.8	20I95	160.0	7.8	15.0	3.03	1.67
156.0	14WF111	176.3	15.8	40.2	1.13	4.05							
148.4	33WF141	446.8	12.5	15.1	3.01	2.84							

* Non-compact section

TABLE 1 (A36 steel)

C	Shape	S	L _c	L _u	d/A _f	r'	C	Shape	S	L _c	L _u	d/A _f	r'
52.8	14WF68	103.0	10.9	23.3	1.95	2.74	15.2	8WF35	31.1	8.7	22.2	2.05	2.21
52.7	*12WF65	88.0	13.0	30.0	1.67	3.31	15.2	12I50	50.3	5.9	13.7	3.32	1.29
52.1	8WF67	60.4	9.0	39.2	1.16	2.29	15.0	15I50	64.2	6.1	10.6	4.28	1.30
51.9	24I100	197.6	7.9	11.9	3.81	1.63	14.2	16WF40	64.4	7.6	10.0	4.54	1.76
50.3	27WF84	211.7	10.8	10.8	4.21	2.40	13.5	*8BP36	29.9	8.8	22.6	2.21	2.20
48.7	16WF61	115.9	9.3	19.1	2.38	2.21	13.4	15I42.9	58.9	6.0	10.4	4.39	1.29
48.6	20I85	150.2	7.6	14.7	3.09	1.67	13.4	14WF38	54.6	7.3	11.2	4.06	1.72
48.0	24I90	185.8	7.7	11.7	3.87	1.63	13.3	12WF36	45.9	7.1	13.2	3.45	1.70
46.8	18WF70	128.2	9.5	16.6	2.74	2.25	13.3	8M34.3	28.9	8.7	20.8	2.18	2.07
45.0	24WF76	175.4	9.7	11.7	3.90	2.22	12.9	12I40.8	44.8	5.7	13.1	3.47	1.27
45.0	10WF60	67.1	10.9	30.5	1.49	2.79	12.8	8M32.6	28.2	8.6	20.6	2.20	2.06
44.1	24I79.9	173.9	7.6	11.5	3.94	1.64	12.4	*10WF33	35.0	8.6	17.7	2.83	2.17
43.6	21WF73	150.7	9.0	13.1	3.46	2.08	12.0	18WF40	68.3	6.5	8.0	5.68	1.53
42.7	14WF61	92.2	10.8	21.0	2.16	2.72	11.9	*8WF31	27.4	8.7	21.6	2.31	2.20
41.1	12WF58	78.1	10.8	23.9	1.90	2.76	11.6	21WF44	81.5	—	6.4	7.05	1.59
39.6	16WF64	104.2	9.2	17.3	2.63	2.19	10.6	16WF36	56.3	7.6	8.6	5.30	1.72
39.4	8WF58	52.0	8.9	34.4	1.32	2.27	10.6	14WF34	48.5	7.3	9.9	4.58	1.70
39.1	18WF64	117.0	9.4	15.2	2.99	2.23	9.9	12WF31	39.4	7.1	11.4	3.98	1.68
37.5	21WF68	139.9	9.0	12.2	3.73	2.07	9.14	8WF28	24.3	7.1	17.1	2.66	1.79
37.1	10WF54	60.4	10.9	27.9	1.63	2.78	8.75	10WF29	30.8	6.3	12.9	3.52	1.51
33.9	*10BP57	58.9	11.1	28.8	1.74	2.76	8.71	12I35	37.8	5.5	10.5	4.34	1.19
33.8	12WF53	70.7	10.8	21.7	2.09	2.74	8.42	18WF35	57.9	6.5	6.6	6.88	1.50
33.7	24WF68	153.1	9.7	10.0	4.55	2.17	8.16	12I31.8	36.0	5.4	10.3	4.41	1.19
32.3	16WF58	94.1	9.2	15.6	2.91	2.17	7.78	14WF30	41.8	7.3	8.5	5.37	1.66
31.8	20I75	126.3	6.9	11.4	3.97	1.47	7.48	6M25	15.7	6.4	21.6	2.10	1.55
31.0	18WF60	107.8	8.2	13.1	3.48	1.91	7.45	8M28	22.5	7.2	15.1	3.02	1.69
30.5	21WF62	126.4	8.9	11.0	4.15	2.04	7.41	12WF27	34.1	7.0	9.9	4.60	1.65
30.5	*10WF49	54.6	10.8	28.0	1.79	2.76	7.30	6WF25	16.8	6.6	19.7	2.30	1.67
29.9	*12BP53	67.0	13.1	22.3	2.24	3.25	7.24	16B31	47.0	6.0	7.0	6.49	1.36
29.6	14WF53	77.8	8.7	17.3	2.63	2.17	7.09	10I35	29.2	5.4	11.0	4.12	1.13
28.9	20I65.4	116.9	6.8	11.2	4.05	1.47	6.80	8M24	21.0	7.0	14.7	3.09	1.69
28.2	8WF48	43.2	8.8	29.7	1.53	2.25	6.78	8WF24	20.8	7.0	14.8	3.07	1.79
27.5	12WF50	64.7	8.8	19.3	2.53	2.20	6.47	10WF25	26.4	6.2	11.1	4.08	1.49
25.7	18WF55	98.2	8.2	11.9	3.82	1.90	6.21	10M29.1	26.6	6.4	10.6	4.28	1.38
24.4	18I70	101.9	6.8	10.9	4.17	1.40	5.58	10I25.4	24.4	5.0	10.4	4.37	1.12
24.2	14WF48	70.2	8.7	15.7	2.90	2.16	5.34	10M22.9	23.6	6.2	10.3	4.42	1.38
24.1	10WF45	49.1	8.7	22.3	2.04	2.20	5.28	14B26	34.9	5.4	6.9	6.61	1.25
22.7	24WF61	129.5	7.6	8.0	5.71	1.72	5.27	6M22.5	13.7	6.6	17.5	2.60	1.52
22.6	21WF55	109.7	8.9	9.4	4.85	2.00	4.85	6M20	12.9	6.4	17.1	2.66	1.52
22.4	12WF45	58.2	8.7	17.5	2.60	2.18	4.77	6WF20	13.4	6.5	16.2	2.81	1.65
22.1	16WF50	80.7	7.7	12.4	3.66	1.80	4.62	16B26	38.0	—	5.5	8.25	1.31
21.1	18WF50	89.0	8.1	10.8	4.22	1.88	4.24	10WF21	21.5	6.2	9.0	5.07	1.44
20.3	18I54.7	88.4	6.5	10.4	4.35	1.40	4.17	8WF20	17.0	5.7	11.1	4.08	1.36
19.4	14WF43	62.7	8.7	14.0	3.24	2.15	4.15	10M21	21.1	6.2	9.2	5.09	1.41
19.4	8WF40	35.5	8.8	24.8	1.83	2.23	4.09	5WF18.5	9.94	5.4	18.7	2.43	1.39
18.8	*10BP42	43.4	10.9	21.7	2.31	2.72	4.06	8M22.5	17.1	5.8	10.8	4.21	1.76
18.0	12WF40	51.9	8.7	15.7	2.89	2.17	3.96	5WF18.9	9.5	5.4	18.9	2.40	1.31
17.9	10WF39	42.2	8.7	19.3	2.36	2.19	3.58	8M18.5	15.5	5.7	10.5	4.33	1.27
17.8	16WF45	72.4	7.6	11.2	4.07	1.78	3.55	8I23	16.0	4.5	10.1	4.51	0.978
17.0	24WF55	113.7	—	6.8	6.69	1.69	3.52	14B22	28.8	5.4	5.6	8.19	1.21
16.5	18WF45	78.9	8.1	9.5	4.79	1.85	3.51	12B22	25.3	4.4	6.3	7.20	1.02
15.5	21WF49	93.2	—	7.6	6.00	1.62	3.11	8M20	15.2	5.8	9.3	4.89	1.27
							3.07	5WF16	8.53	5.4	16.3	2.78	1.38
							3.01	8I18.4	14.2	4.3	9.7	4.71	0.969
							2.91	10B19	18.8	4.4	7.0	6.47	1.03
							2.85	8WF17	14.1	5.7	9.2	4.95	1.33

* Non-compact section

TABLE 1 (A36 steel)

<i>C</i>	Shape	<i>S</i>	<i>L_c</i>	<i>L_u</i>	<i>d/A_f</i>	<i>r'</i>	<i>C</i>	Shape	<i>S</i>	<i>L_c</i>	<i>L_u</i>	<i>d/A_f</i>	<i>r'</i>
2.80	8M17	14.0	5.7	9.1	5.00	1.27	1.29	5I14.75	6.0	3.6	9.7	4.67	0.771
2.72	*6WF15.5	10.1	6.5	13.5	3.72	1.63	1.26	8B13	9.88	4.3	5.8	7.87	1.00
2.63	6B16	10.1	4.4	11.8	3.84	1.08	1.11	12B14	14.8	—	3.4	13.4	0.941
2.60	7I20	12.0	4.2	9.8	4.62	0.885	0.939	5I10	4.8	3.3	8.9	5.11	0.729
2.46	12B19	21.4	4.3	5.2	8.69	0.994	0.854	*10B11.5	10.5	—	4.1	12.3	0.960
2.13	7I15.3	10.4	4.0	9.3	4.88	0.893	0.792	*8B10	7.79	—	5.1	9.83	1.00
2.11	10B17	16.2	4.3	5.9	7.67	1.01	0.690	12JR11.8	12.0	—	2.6	17.4	0.691
1.90	4M13	5.2	4.2	16.6	2.73	1.03	0.675	4I9.5	3.3	3.0	9.3	4.89	0.673
1.86	6I17.25	8.7	3.9	9.7	4.69	0.825	0.664	*6B8.5	5.07	—	6.6	7.63	0.321
1.84	4WF13	5.45	4.4	15.3	2.97	1.10	0.585	4I7.7	3.0	2.9	8.9	5.13	0.659
1.83	8B15	11.8	4.3	7.1	6.44	1.03	0.431	10JR9.0	7.8	—	2.5	18.1	0.617
1.63	14B17.2	21.0	—	3.5	12.9	0.922	0.413	3I7.5	1.9	2.7	9.9	4.60	0.609
1.56	12B16.5	17.5	—	4.1	11.2	0.959	0.343	3I5.7	1.7	2.5	9.2	4.95	0.583
1.49	10B15	13.8	4.3	4.9	9.29	0.985	0.253	8JR6.5	4.7	—	2.4	18.6	0.531
1.45	6I12.5	7.3	3.6	9.1	5.02	0.802	0.187	7JR5.5	3.5	2.3	2.4	18.7	0.493
1.35	6B12	7.24	4.3	8.4	5.38	1.04	0.126	6JR4.4	2.4	2.0	2.4	19.0	0.448

* Non-compact section

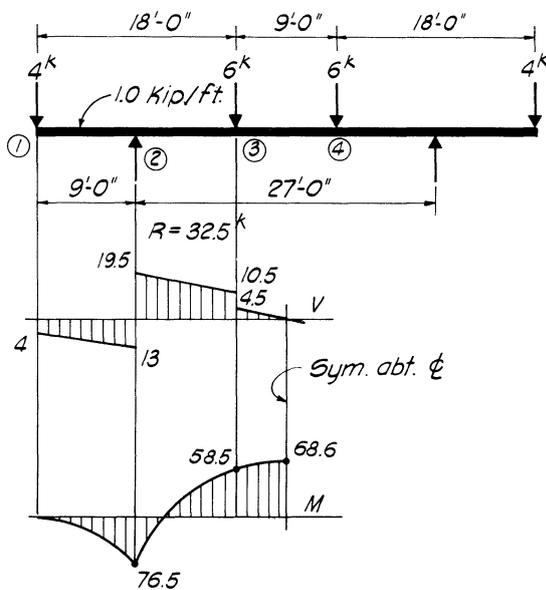


Figure 2

Example 2—Select the most economical beam for the span and load condition illustrated in Fig. 2. Lateral supports are provided at 9-ft intervals between the supports and continuous for the free ends. Use A36 steel.

Solution:

The points of application of load and points of vertical support are also points of support against lateral buckling. The critical buckling section is the region of high positive moment between points of lateral support (3) and (4), and the maximum positive moment should be used to determine the required value of *C*.

From Equation (1),

$$C = \frac{12 \times 68.6 \times 9}{1,000} = 7.41$$

The points of maximum negative moment are critical sections as far as maximum allowable stress ($F_b = 0.60F_y$) is concerned; therefore, maximum negative moment should be used to determine the required *S*.

$$\text{Req'd } S = 76.5 \times \frac{12}{22} = 41.7 \text{ in.}^3$$

1. The minimum required *C* as computed by Equation (1) is 7.41. The minimum required *S* is 41.7 in.³. Select from Table 1 sections with *C*-values equal to or greater than the required *C*, having values of *S* equal to or greater than the required *S*, until the most economical section is determined.

From Table 1:

<i>C</i>	Shape	<i>S</i>	<i>L_c</i>	<i>L_u</i>	<i>d/A_f</i>	<i>r'</i>	Re- marks
8.71	12I35	37.8	5.5	10.5	4.34	1.19	NG
8.42	18WF35	57.9	6.5	6.6	6.88	1.50	OK
8.16	12I31.8	36.0	5.4	10.3	4.41	1.19	NG
7.78	14WF30	41.8	7.3	8.5	5.37	1.66	USE
7.48	6M25	15.7	6.4	21.6	2.10	1.55	NG
7.45	8M28	22.5	7.2	15.1	3.02	1.69	NG
7.41	12WF27	34.1	7.0	9.9	4.60	1.65	NG

Select the 14WF30 as the lightest section having the required *C* and *S* values.

2. For normal cases, calculations need go no further. However, for illustrative purposes, check the 14WF30 with $S = 41.8$, $r' = 1.66$, $d/A_f = 5.37$.

$$C_{b\ 1-2} = 1.75 \text{ for cantilever ends}$$

$$\begin{aligned} C_{b\ 2-3} &= 1.75 - 1.05 \left(-\frac{58.5}{76.5} \right) + 0.3 \left(-\frac{58.5}{76.5} \right)^2 \\ &= 2.82 \text{ (use 2.3)} \end{aligned}$$

$$C_{b\ 3-4} = 1$$

Formula (4):

$$F_{b\ 1-2} = 22,000 - \frac{0.679}{1.75} \left(\frac{9 \times 12}{1.66} \right)^2 = 20.36 \text{ ksi}$$

$$F_{b\ 2-3} = 22,000 - \frac{0.679}{2.3} \left(\frac{9 \times 12}{1.66} \right)^2 = 20.75 \text{ ksi}$$

$$F_{b\ 3-4} = 22,000 - \frac{0.679}{1} \left(\frac{9 \times 12}{1.66} \right)^2 = 19.12 \text{ ksi}$$

Formula (5):

$$F_b = \frac{12,000,000}{9 \times 12 \times 5.37} = 20.7 \text{ ksi}$$

3. The permitted allowable stress is 20.7 ksi, the largest of the values computed by Formulas (4) and (5).

$$f_{\text{actual}} = \frac{68.6 \times 12}{41.8} = 19.7 < 22.0 \text{ ksi} \quad \mathbf{OK}$$

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