# AISC Column Design Logic Makes Sense for Composite Columns, Too

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STRUCTURAL engineers of North America have regarded the composite column generally as a curious stepchild who does not quite belong to a family, yet appears to behave very well. Fathers of the American Concrete Institute have provided shelter by permitting their own ACI routines to be applied to "concrete compression members reinforced longitudinally with structural steel shape, pipe, or tubing."<sup>1</sup> As a "concrete compression member" the stepchild is restrained from doing its own thing as effectively as its structural steel cousins are allowed to do. The ACI Building Code forbids consideration of axially loaded columns by insisting that all columns also function as beams.

Within the structural steel shape<sup>2</sup> and tubing<sup>3</sup> family, compression members can be assembled for design as axially loaded columns. Composite columns that are incorporated into structures with connections identical to those used for steel shapes or tubes ought to be considered analytically to behave exactly the same as the shapes or tubes.

Composite columns possess better stiffness and local stability than their structural steel cousins, and they are much more reliable in shear and ductility than their reinforced concrete cousins. Even though they cost more to produce than either of the cousins, their potential benefit-cost ratio may make them a far more attractive sibling for any structural family—whether it be concrete, steel, or a new genre as yet unnamed. The following demonstration of composite column analysis and comparison with laboratory behavior is intended to encourage the steel family to consider the adoption of design rules for composite columns.

### AXIALLY LOADED COMPOSITE COLUMNS

The logic of the AISC Specification can be applied to axially loaded composite columns if the influence of concrete on the strength, stiffness, and cross-section slenderness of composite columns is incorporated into effective parameters  $F_y^*$  for strength,  $E^*$  for stiffness and  $r^*$  for composite section radius of gyration. Definitions of each equivalence parameter follow:

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$$F_{y}^{*} = F_{y} + 0.85 f_{c}^{\prime} \frac{A_{c}}{A_{s}}$$
(1)

$$E^* = E_s + E_c \frac{A_c}{A_s} \tag{2}$$

$$r^* = \sqrt{\frac{E_s I_s + 0.5 E_c I_c}{E_s A_s + 0.5 E_c A_c}}$$
(3)

in which

- $A_c$  = area of concrete in composite cross section
- $A_s$  = area of steel in composite cross section
- $E_c$  = modulus of elasticity for concrete
- $E_s$  = modulus of elasticity for steel
- $f'_c$  = design compressive strength of concrete standard cylinders
- $F_{y}$  = static yield strength of steel
- $I_c$  = moment of inertia of concrete in composite cross section
- $I_s$  = moment of inertia of steel in composite cross section

These parameters were applied to 84 concrete-filled tube columns and 30 concrete-encased rolled-shape columns that had been tested in recent years.<sup>4,5,6,7,8</sup> The parameters were then used in AISC column strength formulas in order to compute "allowable" loads on each of the 114 specimens. Significant computed quantities are listed in Tables 1 and 2.

The AISC strength formulas take the following form with the modified parameters:

$$C_c = \pi \sqrt{\frac{2E^*}{F_y^*}} \tag{4}$$

where  $C_c$  is the slenderness ratio dividing elastic from inelastic buckling. When the effective length Kl is less than the product  $r^*C_c$ , the axial stress  $F_a$  should be computed:

$$F_{a} = \frac{\left[1 - \frac{1}{2} \left(\frac{Kl}{r^{*}C_{c}}\right)^{2}\right] F_{y}}{\frac{5}{3} + \frac{3}{8} \frac{Kl}{r^{*}C_{c}} - \frac{1}{8} \left(\frac{Kl}{r^{*}C_{c}}\right)^{3}}$$
(5)

							Kl			Ptest
Ref.	O.D. (in.)	$A_{s}$ (in. <sup>2</sup> )	$A_c$ (in. <sup>2</sup> )	f <sub>y</sub> (ksi)	<i>f</i> ' <sub>c</sub> (ksi)	<i>Kl</i> (in.)	$\overline{r^*C_c}$	$P_{ax}$ (kips)	P <sub>test</sub> (kips)	$\frac{P_{ax}}{P_{ax}}$
	3.74	5.07	5.92	39.9	2.94	33.9	0.353	113.0	229.0	2.02
						55.9	0.582	96.9	209.0	2.16
						78.0	0.812	76.4	203.0	2.66
	3.74	1.63	9.36	50.7	3.62	33.9	0.383	57.3	150.0	2.62
						78.0	0.882	35.6	119.0	3.34
	8.50	4 99	52.5	42.3	3.32	87.4	0.421	164.0	371.0	2.26
	0.00			41.7	4.32	87.4	0.443	182.0	509.0	2.79
	8.50	6.13	50.6	56.8	3.32	87.4	0.453	241.0	549.0	2.27
				50.8	4.32	87.4	0.449	245.0	645.0	2.63
	3.74	1.63	9.36	49.0	3.49	80.0	0.890	34.0	104.0	3.06
ner	4.76	2.14	15.6	45.2	3.06	41.3	0.348	72.0	162.0	2.25
ard					3.51	41.3	0.354	51.0	192.0	2.54
d G					3.51	91.0	0.781	53.0	163.0	3.08
, an	4.76	3.11	14.7	49.8	3.06	41.3	0.359	100.6	227.0	2.26
sen					3.51	41.3	0.354	99.7	245.0	2.46
cob					3.06	91.0	0.791	69.8	180.0	2.58
;, Ja	1.00	0.11	0.69	7.0.0	3.51	91.0	0.781	69.9	195.0	2.79
gnol	1.00	0.11	0.68	76.0	4.04	42.0	1.44	1.31	3.52	2.69
<sup>r</sup> url	1.50	0.48	1.29	76.0	4.04	42.0	1.00	10.7	24.7	2.31
ni, I	2.00	0.40	2.74	76.0	4.04	42.0	0.736	15.5	27.1	1.77
alaı	3.00	19.7	0.47	51.5	5.50	42.0	0.474	010.0	2576.0	2.24
ck, Sims and C	14.00	10.7	135.0	51.5	4.76	22.0	0.165	361.0	2408.0	2.80
	14.00	8.07	146.0	40.1	3.04	21.1	0.153	402.0	791.0	1.97
	14.00	13.50	140.0	51.5	3.40	21.5	0.187	622.0	1671.0	2.69
	5.01	0.99	18.7	53.8	9.6	19.7	0.222	115.0	289.0	2.49
l Pai				47.7	9.6	19.7	0.218	112.0	289.0	2.58
and	5.00	1.78	17.9	53.8	9.6	20.0	0.206	136.0	293.0	2.15
/les				47.7	9.6	20.0	0.201	130.0	293.0	2.25
now	4.00	1.49	11.1	87.8	4.95	60.0	0.566	80.2	184.0	2.29
, K	4.70	0.00	1	CF F	4.52	60.0	0.563	/8.6	180.0	2.29
oden	4.70	2.33	15.5	65.5	4.99	41.3	0.245	121.0	260.0	2.16
ĽČ					3.76	41.3	0.286	109.0	210.0	1.96
anc	6.00	2.29	26.0	60.2	3.03	66.0	0.348	107.0	211.0	1.85
pel									198.0	2.39
tlöp	3.01	0.63	6.5	52.7	3.62	60.0	0.616	23.0	55.0	2.57
× k					5.93	24.0	0.266	36.0	92.5	2.51
sts h	4.50	1 79	14.9	60.0	3.70	24.0	0.240	29.0	160.0	1.89
Tes	4.50	1.72	14.4	00.0	4.20	55.0	0.238	04.5	170.0	2.01
7.	5.00	1.46	18.2	42.0	5.10	59.0	0.346	81.7	141.0	1.73
.ef.									140.0	1.71
К									148.0	1.81
	6.00	1.14	27.1	48.0	3.05	59.0	0.303	72.9	153.0	2.10
					3.75	59.0	0.312	82.2	162.0	1.97
	5 51	6 14	17 7	38 5	4 66	16.0	0.079	181.0	663.0	2.01
	5.51	0.17	11.1.1	39.0	4.66	16.0	0.079	183.0	663.0	3.63
	5.53	3.25	20.8	41.9	4.74	16.0	0.079	130.0	410.0	3.15
				43.2	4.74	16.0	0.079	132.0	410.0	3.10
	6.62	3.62	30.8	43.2	4.56	32.0	0.139	160.0	451.0	2.81
					6.26	32.0	0.152	184.0	502.0	2.73
					2 21	32.0	0.127	141.0	475.0	2.58
					3.34	54.0	0.137	141.0	592.0	2.19

Table 1. Axially Loaded Steel Tubes Filled with Concrete

		. (1 2)	. (1 2)				Kl			P <sub>test</sub>
Ref.	O.D. (in.)	$A_{s}(\text{in.}^{2})$	$A_c$ (in. <sup>2</sup> )	$f_y$ (ksi)	$f_c$ (ksi)	Kl (in.)	r*C <sub>c</sub>	$P_{ax}$ (kips)	P <sub>test</sub> (kips)	Pax
Ref. 7. (cont'd)	3.50	2.36	7.26	58.0	5.81 5.75	68.0 56.0	0.758 0.625	64.9 74.1	138.0 160.0	2.13 2.16
			7.74	70.0	5.65 6.06 5.92	44.0 32.0 20.0	0.491 0.358 0.223	81.6 90.8 96.6	161.0 206.0 223.0	1.97 2.27 2.31
	3.50	0.55			6.00 5.36 5.92	68.0 56.0 44.0 32.0 20.0 10.0	$\begin{array}{c} 0.805\\ 0.638\\ 0.512\\ 0.372\\ 0.232\\ 0.116\end{array}$	$27.7 \\ 31.4 \\ 36.6 \\ 40.1 \\ 43.1 \\ 45.1$	50.5 66.2 80.0 90.0 110.0 119.2	$1.82 \\ 2.11 \\ 2.19 \\ 2.24 \\ 2.55 \\ 2.64$
Ref. 6. Spiral steel tubes tested by Gardner	6.64	2.13	32.5	43.2	2.60 4.95	12.0 78.0 12.0 78.0	0.051 0.333 0.058 0.375	97.2 86.6 136.0	298.0 185.0 274.0 206.0	3.06 2.14 2.01 1.74
	6.64	2.13	32.5	46.0	5.30 4.87	12.0 78.0 12.0 78.0	0.059 0.384 0.058	145.0 125.0 138.0	294.0 170.0 299.0	2.03 1.36 2.17
	6.62	2.89	31.5	32.1	3.86	78.0 12.0 90.0	0.379 0.046 0.345	120.0 117.0 103.0	350.0 213.0	1.29 3.00 2.24
	6.64	3.98	30.6	37.8	4.75	12.0 90.0 12.0	0.048 0.359 0.045	131.0 115.0 163.0	322.0 236.0 442.0	2.46 2.05 2.71
					3.98	90.0 12.0 90.0	0.337 0.044 0.328	$ \begin{array}{r} 145.0 \\ 151.0 \\ 135.0 \end{array} $	254.0 446.0 262.0	$1.75 \\ 2.95 \\ 1.94$

Table 1 (cont'd)

When the effective length Kl is greater than  $r^*C_c$ , the axial stress  $F_a$  should be taken as:

$$F_a = \frac{12}{23} \frac{\pi^2 E^*}{(Kl/r^*)^2} \tag{6}$$

Finally, the allowable axial load  $P_{ax}$  is determined as the product of allowable stress and *steel* area:

$$P_{ax} = F_a A_s \tag{7}$$



Fig. 1. Axially loaded composite columns

The right-hand columns of Table 1 and Table 2 contain ratios of the reported test load  $P_{ax}$  to the computed values  $P_{test}$ . The ratios vary from a low value of 1.29 to a high value of 3.67. The mean value for 114 composite specimens was 2.28, with an 18.4 percent coefficient of variation.

AISC safety factors are intended to be in the range 1.67 to 1.92. The frequency distribution for all 114 tests appears in Fig. 1, and the AISC safety domain is shown as a shaded region of that diagram. The two ratios that were less than 1.40 involved steel tubes fabricated from welded spiral plate stock, and perhaps such tubes require special attention.

### AISC FORMAT FOR BEAM-COLUMNS

Frequently it is necessary to proportion compression members to resist flexural forces in addition to thrust. All columns that are used in frames constructed with moment resistant connections must be considered as beam-columns.

The AISC requirements for designing beam-columns are based on limits to the total stress generated by both thrust and flexure. However, composite columns present

Reference	Concr. Size (in.)	Steel Size (in.)	$A_{s}$ (in. <sup>2</sup> )	$A_c$ (in. <sup>2</sup> )	<i>f'</i> <sub>c</sub> (ksi)	f <sub>y</sub> (ksi)	$\frac{Kl}{r^*C_c}$	P <sub>ax</sub> (kips)	P <sub>test</sub> (kips)	$\frac{P_{test}}{P_{ax}}$
	$5 \times 3.5$	$3 \times 1.5$	1.18	16.32	2.60	36.0	0.398	40.0	81.4	2.04
							0.550	36.0	71.5	1.99
							0.707	31.2	63.0	2.02
							0.864	25.8	43.6	1.69
							1.015	20.0	50.6	2.53
							1.172	15.0	36.1	2.41
sus							1.329	11.6	33.9	2.92
eve	7  imes 6.5	5 imes 4.5	5.88	39.6	1.60	36.0	0.054	177.0	352.0	1.99
' St							0.272	163.0	308.0	1.89
i by							0.490	143.0	317.0	2.22
este							0.707	119.0	288.0	2.42
Ē							0.917	90.6	231.0	2.55
4.	10  imes 8	8  imes 6	10.3	69.7	2.60	36.0	0.472	255.0	568.0	2.22
ef.	$12 \times 10$	8  imes 6	·10.3	110.0	2.60	36.0	0.479	300.0	704.0	2.34
Ř	$14 \times 12$	8  imes 6	10.3	158.0	2.60	36.0	0.441	354.0	836.0	2.42
	$16 \times 12$	12  imes 8	19.1	173.0	2.60	36.0	0.091	627.0	1051.0	1.68
							0.183	608.0	990.0	1.63
							0.274	583.0	926.0	1.59
							0.365	556.0	937.0	1.69
							0.457	525.0	933.0	1.78
	9.5  imes 9.5	5.5 imes5.5	6.66	82.6	4.66	41.5	0.664	255.0	482.0	1.89
nss					4.28	42.7	0.545	268.0	526.0	1.96
Ja					4.77	40.2	0.381	310.0	590.0	1.90
by					4.29	40.0	0.157	271.0	572.0	2.11
sts					4.24	55.0	0.561	294.0	528.0	1.80
Te					4.24	72.6	0.779	298.0	528.0	1.77
					4.27	70.8	0.635	322.0	554.0	1.72
Ę.					4.77	72.5	0.442	384.0	545.0	1.42
Rε					4.39	41.5	0.576	239.0	513.0	2.14
					4.30	70.7	0.694	303.0	517.0	1.71

Table 2. Axially Loaded Encased Steel Shapes

unique problems associated with estimates of stress, either in concrete or in steel. Again a pseudo-allowable bending stress,  $F_b^*$ , can be defined as the product of allowable moment and the steel section modulus, and all other components of AISC design equations can be applied.

The moment capacity of composite cross sections can be determined analytically only by means of rather tedious calculations involving the equilibrium of post-elastic stress conditions associated with compatible strains near ultimate flexural loads. Estimates of a reliable moment capacity  $M_o$  can be taken far more simply by using the product of yield stress and the plastic section modulus of the steel in the cross section of filled tubes and encased shapes that are bent about the major axis. Minor axis bending strength estimates should include not only the weak axis plastic moment for steel, but also the capacity of a concrete section reinforced by the web of the steel shape. For encased shapes bent about the minor axis,

$$M_o = Z_y F_y + A_w F_y \left(\frac{b}{2} - \frac{A_w F_y}{1.7 f_c h}\right) \tag{7}$$

where

- $Z_y$  = weak axis plastic section modulus of rolled shape
- *b* = width of concrete section parallel to steel flanges
- *h* = depth of concrete section in the web direction

 $A_{w}$  = area of web of steel shape

The allowable flexural stress for composite sections should be taken as

$$F_b^* = \frac{3}{5} \frac{M_o}{S} \tag{8}$$

where S = section modulus of steel in plane of bending.

The AISC equation for allowable combinations of thrust and flexural stress then can be used:

$$\frac{f_a}{F_a} + \frac{C_m}{\left(1 - \frac{f_a}{F_e^*}\right)} \times \frac{f_b}{F_b^*} \le 1$$
(9)

Reference	Tube Size (in.)	$A_s$ (in. <sup>2</sup> )	A <sub>c</sub> (in. <sup>2</sup> )	f <sub>y</sub> (ksi)	<sup>f'</sup> c (ksi)	$\frac{Kl}{r^*C_{\mathcal{C}}}$	P <sub>u</sub> (kips)	M <sub>o</sub> (kip-in.)	P <sub>test</sub> (kips)	M <sub>test</sub> (kip-in.)	$\frac{P_{test}}{P_u}$	$\frac{M_{test}}{M_O}$
	4.50 Dia.	1.72	14.2	60.0	4.20	0.238	150	143	100 90 75 50 25	100 106 131 141	0.67 0.60 0.50 0.33	0.70 0.74 0.92 0.99
	6.00 Dia.	1.14	27.1	48.0	3.75	0.318	134	103	128 95 64	88 158 153	0.95 0.71 0.48	0.85 1.52 1.48
		1.40		10.0	3.05	0.308	119	103	30 30	143 133	0.26	1.39
Ref. 9. Tests by Furlong	5.00 Dia. 5.00 Sq.	1.40	18.2 23.2	42.0	6.50	0.288	246	97	$128 \\ 120 \\ 90 \\ 79 \\ 79 \\ 78 \\ 69 \\ 60 \\ 59 \\ 39 \\ 20 \\ 10 \\ 250 \\ 15$	$\begin{array}{c} 78\\ 112\\ 141\\ 140\\ 126\\ 141\\ 151\\ 156\\ 156\\ 146\\ 141\\ 130\\ 310\\ 365\\ 430\\ \end{array}$	0.97 0.91 0.68 0.60 0.59 0.52 0.46 0.44 0.30 0.15 0.07 1.02 0.61 0.61	$\begin{array}{c} 0.82\\ 1.16\\ 1.46\\ 1.45\\ 1.31\\ 1.45\\ 1.56\\ 1.61\\ 1.61\\ 1.51\\ 1.46\\ 1.35\\ 0.67\\ 0.79\\ 0.93\\ \end{array}$
	4.00 Sq.	1.31	14.7	48.0	3.40	0.389	102	93	100 84 84 54 20 20	450 44 45 92 105 114	0.41 0.82 0.82 0.53 0.20 0.20	$\begin{array}{c} 0.98 \\ 0.44 \\ 0.45 \\ 0.92 \\ 1.05 \\ 1.14 \end{array}$
	4.00 Sq.	1.94	14.1	48.0	4.18	0.383	133	135	98 69 68 59 29 29	119 162 162 190 209 193	$\begin{array}{c} 0.74 \\ 0.52 \\ 0.51 \\ 0.44 \\ 0.22 \\ 0.22 \end{array}$	$\begin{array}{c c} 0.88 \\ 1.20 \\ 1.20 \\ 1.41 \\ 1.55 \\ 1.43 \end{array}$

Table 3. Eccentric Loads on Filled Tubes

Again,  $f_a$  and  $f_b$  are to be computed as the total force divided by steel area and total moment divided by steel section modulus, and

$$F_e^* = \frac{12}{23} \frac{E^* \pi^2}{(K/r^*)^2} \tag{10}$$

Results from tests of 37 eccentrically loaded steel tubes filled with concrete were compared with strength estimates adopted from Eq. (9). Specimen characteristics and computed strength values are given in Table 3. The reported flexural capacities already include slenderness effects, and no moment magnification would be appropriate for these filled tube specimens. The axial capacity  $P_u$  was estimated as

$$P_u = F_a A_s \times (F.S.) \tag{11}$$

The ratios  $P_{test}/P_u$  and  $M_{test}/M_o$  are plotted as data points identified by dots in boxes or circles in Fig. 2.





Ref.	Col. Size (in.)	Steel Shape	$A_s$ (in. <sup>2</sup> )	$\begin{array}{c}A_c\\(\text{in.}^2)\end{array}$	f <sub>y</sub> (ksi)	f'c (ksi)	$\frac{Kl}{r^*C_c}$	P <sub>u</sub> (kips)	<i>M<sub>O</sub></i> (kip-in.)	P <sub>test</sub> (kips)	M <sub>test</sub> (kip-in.)	$\frac{P_{test}}{P_u}$	δ	$\frac{\delta M_{test}}{M_O}$
Ref. 5. Janss	9.45 × 9.45	HEB 140	6.66	82.6	41.5 70.7	$\begin{array}{r} 4.80 \\ 4.64 \\ 4.03 \\ 4.50 \\ 4.36 \\ 4.03 \end{array}$	$\begin{array}{c} 0.577 \\ 0.477 \\ 0.569 \\ 0.657 \\ 0.660 \\ 0.659 \end{array}$	511 533 468 617 608 590	512 508 503 819 816 806	251 265 240 265 251 223	394 416 377 416 394 350	$\begin{array}{c} 0.49 \\ 0.50 \\ 0.51 \\ 0.43 \\ 0.41 \\ 0.39 \end{array}$	$     1.37 \\     1.25 \\     1.38 \\     1.41 \\     1.39 \\     1.33 $	1.05 1.03 1.04 0.72 0.67 0.58
	8.27 × 12.60	IPE 220	5.18	99.0	39.5	$\begin{array}{c} 4.64 \\ 4.36 \\ 4.28 \end{array}$	0.509 0.505 0.503	281 271 268	340 338 337	269 234 229	422 367 360	0.52 0.47 0.46	$     \begin{array}{r}       1.31 \\       1.26 \\       1.26     \end{array} $	$     1.62 \\     1.37 \\     1.35   $
Ref. 10. Stevens	12.0 × 16.0	12 × 8 65 lb.	19.1	171.0	32.3	2.52 2.36 2.92 2.68 2.68 2.80 2.72 3.08 3.00	$\begin{array}{c} 0.362 \\ 0.367 \\ 0.353 \\ 0.358 \\ 0.358 \\ 0.354 \\ 0.358 \\ 0.349 \\ 0.350 \end{array}$	961 935 1026 988 988 1007 993 1052 1039	1415 1395 1455 1432 1432 1444 1436 1466 1461	672 486 515 361 296 262 231 199 168	672 972 1032 1083 1184 1310 1386 1393 1344	$\begin{array}{c} 0.70\\ 0.52\\ 0.50\\ 0.36\\ 0.30\\ 0.26\\ 0.23\\ 0.19\\ 0.16\\ \end{array}$	1.40 1.27 1.26 1.18 1.14 1.12 1.11 1.09 1.07	$\begin{array}{c} 0.71 \\ 0.89 \\ 0.90 \\ 0.89 \\ 0.95 \\ 1.02 \\ 1.06 \\ 1.03 \\ 0.99 \end{array}$
Ref. 10. Stevens	6.50 × 7.00	5 × 4½ 20 lb.	5.88	39.6	33.6	2.80	0.492 0.492 0.492 0.492 0.171 0.273 0.273 0.273 0.492 0.710 0.710 0.921 0.921	$\begin{array}{c} 256\\ 256\\ 256\\ 256\\ 287\\ 281\\ 281\\ 256\\ 218\\ 218\\ 168\\ 168\\ 168\\ 168\end{array}$	242 242 242 242 242 242 242 242 242 242	161 168 202 228 166 224 164 141 161 119 99 78 74	121 134 151 183 166 112 164 141 81 119 99 118 148	$\begin{array}{c} 0.63\\ 0.66\\ 0.79\\ 0.89\\ 0.58\\ 0.80\\ 0.58\\ 0.55\\ 0.74\\ 0.55\\ 0.59\\ 0.47\\ 0.44\\ \end{array}$	$\begin{array}{c} 1.36\\ 1.38\\ 1.50\\ 1.61\\ 1.03\\ 1.13\\ 1.09\\ 1.30\\ 2.24\\ 1.69\\ 2.33\\ 1.83\\ 1.75\\ \end{array}$	0.69 0.76 0.93 1.22 0.71 0.52 0.74 0.75 0.74 0.83 0.96 0.90 1.07
Ref. 11. Loke	7.00 × 8.00 7.00 × 8.00	$4 \times 3$ 10 lb. $4 \times 1^{3/4}$ 5 lb.	2.94	53.1	40.7 45.6 39.3 39.5 39.5 42.7 39.5 42.4 42.4 43.0 43.0	$\begin{array}{c} 3.71\\ 3.28\\ 4.20\\ 4.58\\ 4.31\\ 3.25\\ 4.28\\ 4.27\\ 3.91\\ 2.89\\ 3.81\end{array}$	$\begin{array}{c} 0.491\\ 0.502\\ 0.494\\ 0.701\\ 0.697\\ 0.696\\ 0.697\\ 0.500\\ 0.497\\ 0.443\\ 0.455\\ \end{array}$	252 246 268 244 235 206 234 278 264 178 215	152 164 150 152 151 156 151 167 167 89 93	195     108     88     201     135     88     68     211     130     116     108	$78 \\ 86 \\ 132 \\ 40 \\ 54 \\ 70 \\ 101 \\ 84 \\ 104 \\ 46 \\ 86$	$\begin{array}{c} 0.77\\ 0.44\\ 0.33\\ 0.82\\ 0.57\\ 0.43\\ 0.29\\ 0.76\\ 0.49\\ 0.65\\ 0.50\\ \end{array}$	$\begin{array}{c} 1.49\\ 1.24\\ 1.16\\ 1.44\\ 1.27\\ 1.19\\ 1.12\\ 1.49\\ 1.27\\ 1.30\\ 1.23\end{array}$	$\begin{array}{c} 0.76 \\ 0.66 \\ 1.02 \\ 0.37 \\ 0.46 \\ 0.54 \\ 0.75 \\ 0.76 \\ 0.79 \\ 0.52 \\ 1.13 \end{array}$

Table 4. Eccentric Loads on Encased Shapes

Results from 42 eccentrically loaded encased shapes are tabulated in Table 4, together with strength estimates based on Eqs. (9) and (11), except that an ultimate strength moment magnifier  $\delta$  was computed with an effective  $F_e^*$  equal to  ${}^{23}\!/_{12}$  of the value from Eq. (10). The ratios of  $P_{test}/P_u$  and  $\delta M_{test}/M_o$  are plotted as symbols + in Fig. 2.

Data points illustrated in Fig. 2 show that the allowable stress interaction Eq. (9) is definitely valid. When values of  $M_o$  are taken as low as the plastic moment strength of steel tubes filled with concrete, the coefficient  $C_m$  could be taken safely as low as 0.60, with the further restriction that the ratio  $f_b/F_b^* \leq 1$ .

#### SUMMARY

The logic of the AISC Specification can be applied to composite columns that are loaded in either direct or eccentric compression. The proposed relationships for an effective yield strength,  $F_y^*$ , material stiffness,  $E^*$ , and cross-section stiffness,  $r^*$ , will provide for margins of

safety generally larger than those resulting from the AISC column design rules applied to steel alone. The AISC beam-column equations likewise provide a reliable index of capacity. The proposed relationships for estimating flexural strength,  $M_o$ , tend to underestimate actual capacity, particularly for concrete-filled steel tubes.

As the amount or strength of concrete in a composite member is reduced analytically to zero, each of the proposed design equations provides safe estimates for the strength of steel by itself. There remain no transition inconsistencies between the strength of steel alone and the augmented strength from composite action.

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